Introduction to HCAF: Hierarchical Coarray Fortran

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Outline

- Overview
- HCAF Hierarchy Model
- Hierarchical Abstractions
- Language Constructs

Hierarchical Coarray Fortran (HCAF)

- Motivation
 - · Large parallel computers are deeply hierarchical
 - Applications must exploit this hierarchy, not ignore it
- HCAF goals
 - Explicit hierarchical locality in PGAS model
 - Dynamic task and data parallelism
 - Portable performance across machine topologies
 - In the spirit of Fortran
 - Extension of Rice CAF 2.0 with few incompatibilities
- Approach
 - Language exposes hierarchy, programmer exploits it
 - Exposed hierarchies automagically mapped to hardware
- Disclaimers
 - This work is preliminary
 - Still some pending design issues
 - No implementation yet
 - Irregular codes and heterogenous hardware are TBD



HCAF Goals

Hierarchical locality, PGAS, and dynamic parallelism in the spirit of Fortran

What do I mean by "spirit of Fortran"?

- Focus on dense array handling
- Emphasis on performance
- Strong type checking
- Aggressive static optimization

HCAF Design Principles

• Optimizable and manually controllable

- · Programmer makes high-level decisions, can intervene at low level if necessary
- Compiler is responsible for most performance details
- Explicit hierarchical locality
 - Single hierarchy model for hardware, teams, coarrays, task/data parallelism
 - Hierarchy abstraction for locality-aware programming in a hardware-independent way
- Single programming model across all hierarchy levels ("H-PGAS into the node")
 - Teams & coarrays on sets of cores across or within nodes
 - Async, do-parallel, collectives on any team across or within nodes
- Mixed global-view & local-view programming
 - Hierarchical tiling supports both element-wise & tile-wise access (global and local view)
 - · Relative locality redefines coarray local-vs-remote distinction to within-vs-outside current locale
- Strong typing and statically known locality
 - Type system captures hierarchical structure of teams and coarrays
 - Static correctness checking of hierarchy references (e.g. subscript rank)
 - Static locality-aware optimization
 - Dynamic hierarchy supported by runtime checking

Related Work

- Hierarchically Tiled Arrays and HPF
 - HTA's are *hierarchical*, but *dynamic tiling* \Rightarrow no static optimization
 - HPF has static tiling info => aggressive optimization, but not hierarchical
 - HCAF: hierarchical tiling with static info for locality optimization
- Hierarchical Place Trees and Titanium Hierarchical Teams
 - HPTs model locality only intra-node and are global & fixed at startup
 - Titanium teams are programmable & modular, but model only inter-image locality
 - HCAF: programmable, modular teams extending inter-node to intra-image
- Topology Mapping
 - Two approaches: graph-based (LibTopoMap) and tree-based (TreeMatch, Rubik)
 - TreeMatch maps arbitrary-size trees, but trees are unordered
 - Rubik uses Cartesian topologies but maps same-size trees
 - HCAF: maps arbitrary-size trees with Cartesian topologies
- **Dynamic Parallelism & Work Stealing** (X10, Habanero, HotSLAW et al)
 - Locality-aware fork-join parallelism + parallel loops based on fork-join
 - Sophisticated inter- and intra-node *hierarchical work stealing* algorithms
 - HCAF: same, but with more static info for locality optimization

Opportunity: Statically-known Hierarchical Tiling

[Our] current implementation as a library forces to use dynamic analysis techniques to determine the communication patterns required when data is to be shuffled among processors. A compiler could calculate statically those patterns when they are regular enough, and generate a code with less overhead.

"Programming for Parallelism and Locality with Hierarchically Tiled Arrays", Bikshandi et al, 2006. (emphasis added)

Cross-component optimization is essential to attain reasonable performance. For languages like HPF, compilers synthesize message passing communication operations and manage local buffers. Interprocedural analysis can reduce the frequency and volume of communication significantly. In the HTA library, communication optimization is in the hands of the programmer. A possible concern is that the programmer may not use the library efficiently.

> "Optimization Techniques for Efficient HTA Programs", Fraguela, Bikshandi, et al, 2012. (summarized)

Opportunity: Machine-independent Explicit Locality



all hierarchical

- Locale denotes a relatively compact subset of hardware
- Team provides abstraction of hardware subset with desired topology
- Coarray exposes data locality for explicit management by application
- Map M₁ distributes data over application topology
- Map M₂ embeds application topology into physical topology

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- Overview
- HCAF Hierarchy Model
 - Resource hierarchies
 - Hierarchy maps
 - Hierarchy patterns
- Hierarchical Abstractions
- Language Constructs
- Implementation Ideas

Hierarchy: Basic Concepts

- Hierarchy here means recursive partitioning
 - ... of a finite set

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- Each set in the hierarchy has an associated partition into subsets
- A hierarchy may be viewed as a tree of sets in two ways
 - Consider the hierarchy { { { 1}, {2} }, { {3}, {4}, {5} } }
 - T1 has nodes labeled with *included* sets
 - T₂ has leaves labeled with *owned* sets; an interior node's included set is the union of its children's included sets
 - We use T1 for natural global / local view, but T2 describes hardware
- HCAF uses hierarchies to represent *locality*
 - A subtree denotes a *neighborhood* of things *relatively close* together
 - A node's children subdivide it into *smaller, closer* neighborhoods
- Tiling here means rectangular partitioning
 - ... of a rectangular *n*-dimensional grid into *tiles*, also rectangular
 - A tiling may be *nonaligned*, *aligned*, or *regular* [1]
- Hierarchical tiling means recursive rectangular partitioning
 - Each tile is partitioned into a set of *sub-tiles*
 - Can be viewed as a hierarchy or tree with *rectangular structure*











hierarchical, regular

Cartesian Resource Hierarchies

- The structure underlying locales, teams, and coarrays •
- A Cartesian resource hierarchy is a tuple (V, E, $\{A_r\}, \mathcal{K}$) where ٠
 - (V, E, A) is a rooted attributed tree with $A = \{A_r\} \cup \{\mathcal{K}\}$
 - Each A_r is a *resource attribute function* of type R_r •
 - $\mathcal K$ is the topology function which assigns to each interior node $n \in V$ with children C_n a Cartesian topology $\mathcal{K}(n)$ for C_n
- A resource attribute function of type R is some $f: V \rightarrow \mathcal{P}(R)$ ٠ where
 - R is a finite set of resource elements and $\mathcal{P}(R)$ is the power set of R
 - $\forall n \in V$ with children C_n : $\{f(c) \mid c \in C_n\}$ is a partition of f(n)
 - \forall leaf $n \in V$: f(n) is a singleton
- A Cartesian topology for V is a function $t : \mathcal{D}_k \rightarrow V$ where
 - t is one-to-one (need not be onto)
 - $\mathcal{D}_k = \prod_i [L_i, U_i]$ is a k-dimensional Cartesian domain (ie with rank k)
 - $\{L_i\}$ and $\{U_i\}$ are the lower and upper bounds of \mathcal{D}_k
 - The shape of the topology is $(U_1 L_1, U_2 L_2, \dots, U_k L_k)$



f:	
$r \mapsto \{1, 2, 3, 4, 5, 6, 7, 8\}$	f ↦ {4 }
<i>a</i> ↦ {1,2,3,4}	g ↦ {5}
<i>b</i> → {5,6,7,8}	h ↦ {6 }
c ↦ {I}	i ↦ {7 }
d ↦ {2}	j ↦ {8 }
e ↦ {3}	

\mathcal{K} (r) :	\mathcal{K} (a) :	\mathcal{K} (b) :
(I) → a	(I,I) ⊢ c	(I,I) → g
(2) ↦ <i>b</i>	(2,I) ↦ d	(2,I) ↦ h
	(I,2)	(1,2) ↦ i
	(2,2) ↦ f	(2,2) ↦ j

Characterization of Cartesian Hierarchies

- A *d-uniform* hierarchy is one where every leaf has depth *d*
- A d-ranked hierarchy is one where
 - Every leaf node has depth $\geq d$
 - $\forall d' \leq d \exists k_{d'}$ s.t. every node of depth d' has a topology of rank $k_{d'}$
 - Then the *d*-rank of the hierarchy is $(k_0, k_2, \dots, k_{d-1})$
 - A *ranked* hierarchy is *d*-ranked and *d*-uniform for some *d*; then ($k_0, k_2, \ldots, k_{d-1}$) is its rank
- A *d-regular* hierarchy is one where
 - The hierarchy is *d*-ranked
 - $\forall d' \leq d \exists S_{d'}$ s.t. every node of depth d' has a topology of shape $S_{d'}$
 - Then the *d-shape* of the hierarchy is $(S_0, S_2, \dots, S_{d-1})$
 - A regular hierarchy is *d*-regular and *d*-uniform for some *d*; then (S₀, S₂, ... S_{*d*-1}) is its shape
- HCAF uses these properties for security and efficiency:
 - · Locales and teams are ranked; coarrays are regular
 - Types of hierarchical objects have *d-rank type parameters* for type checking and optimization of subscripts and loops



regular hierarchy of depth 2 hierarchy rank = (1, 2) hierarchy shape = ((2), (2, 2))

Tiled Resource Hierarchies

- A tiled resource hierarchy is a tuple (V, E, \mathcal{K} , {A_r}, \mathcal{T}) where
- (V, E, \mathcal{K} , {A_r}) is a Cartesian resource hierarchy
- $A_t \in \{A_r\}$ is the *tiled resource* of type R_t

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- T is the tiling function, a resource attribute assigning to each node $n \in V$ a Cartesian topology T(n) for $A_t(n)$ which satisfies certain conditions
- R_t is the set of **tiled elements**, $A_t(n) \subset R_t$ is the **tile** at n, and $\mathcal{T}(n)$ is the **element topology** at n
- T(n) specifies an index tuple for each tile element of *n*'s tile
- \mathcal{T} must satisfy tiling conditions at every $n \in V$ with children C_n :
- $\{\mathcal{T}(c) \mid c \in C_n\}$ is a partition of $\mathcal{T}(n)$, viewing the functions as sets of pairs
- The tile at *n* has rank *k* and bounds [*L_i*] and [*U_i*] of \mathcal{D}_k , where $\mathcal{T}(n) : \mathcal{D}_k \to V$
- Thus a given tile element has the same indices at every level of tiling;
 HCAF uses this convention for subscripting teams and coarrays
- Rank and shape are defined for both elements and tiles at a node:
 - We use rank, shape, and size for the element-wise topology at a node
 - We use corank, coshape, and cosize for the tile-wise topology at a node



uniform hierarchy of depth 2 hierarchy rank = (1, 2) hierarchy shape = ((2), (2, 2))





Hierarchy Maps

- A hierarchy map M from G to H is a tuple (G, H, m) where
 - m: V_G → P(V_H) is descendant-preserving, i.e.
 if p, q ∈ V_G and p is a descendant of q, then
 ∀r ∈ m(p) ∃s ∈ m(q) such that r is a descendant of s
 - This preserves our notion of locality (relative closeness)
 - · Cartesian topologies are not preserved, but should be "respected"
- Hierarchy maps adapt an application's virtual hierarchies to fit the current job's hardware hierarchy
 - A hierarchical team is mapped to a set of processors (with corresponding hierarchical structure)
 - A hierarchical coarray is mapped to a set of memories (with corresponding hierarchical structure)
 - Hierarchy map composition provides modularity:
 e.g. if H is the hardware and G is a team passed to a library, the library realizes its preferred team structure G₂
 by composing a new map with G's existing map:

 $G_2 \rightarrow G \rightarrow H$

- Goodness of maps and finding good ones are TBD
 - But there are many relevant papers & working systems



t is a descendant of s $m(t) = \{b, d\}, m(s) = \{a\}$ b is a descendant of a \checkmark d is a descendant of a \checkmark





Hierarchy Map Examples



coarse to fine



shallow to deep



low to high rank





fine to coarse

deep to shallow

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high to low rank

Goodness of Hierarchy Maps





Goodness of Hierarchy Maps



- Best mapping between a given pair of hierarchies may not be great
 - How serious this is depends on the situation
 - E.g. the map above may be fine if all target locales are shared-memory
- For best results: choose a source hierarchy that maps well to target
- HCAF's answer for this is tiling patterns

Tiling Patterns

- A tiling pattern is a pair P = (R, M) where
 - R = (ko, k2, ... kd-1) is a d-rank
 - *M* is a possibly infinite set of tiled resource hierarchies with d-rank *R*, comprising all the matches of *P*
- A matching function is some Match : (P, \mathcal{D}_k , H_T) \mapsto (H_0 , m) where
 - $P = ((k_0, k_2, \dots, k_{d-1}), M)$ is the tiling pattern to be matched
 - \mathcal{D}_k is the *input domain*, a Cartesian domain with rank $k = k_0$
 - H_T is the target hierarchy, a tiled resource hierarchy that the match result should conform to
 - $H_0 \in M$ is the *output hierarchy*, a tiled resource hierarchy satisfying:
 - $H_R \in M$, i.e. the output hierarchy matches the pattern P
 - Domain(T(r)) = D_k, where r is the root of H₀;
 i.e. the top level tile of H₀ is the input domain,
 i.e. the input domain is tiled by P to give the output hierarchy
 - *m* is the output hierarchy map from H_R to H_T ; i.e. a view of the output hierarchy as an abstraction of the target
- Of course we prefer that *m* be a *good* hierarchy map





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- HCAF Hierarchy Model
- Hierarchical Abstractions
 - Locales: machine topology
 - Teams: processor groups
 - Coarrays: data objects
- Language Constructs

Locales: Hierarchical Machine Topology

- Locales are units of computer hardware locality
 - Nested regions of a parallel computer containing computing resources which are *relatively close* in terms of *communication cost*
 - E.g. cores, dies, sockets, nodes, boards, chassis, cabinets, ...
- A locale is a Cartesian resource hierarchy (V, E, A, \mathcal{K}) where
 - V is the set of regions and E is the containment relation among them
 - A = {Procs, Mems, Comm} describes each locale's computing elements
 - **Procs** : $V \rightarrow \mathcal{P}(P)$ is the processor resource function
 - *P* is the set of processors (hardware threads)
 - $Procs(e) = \{p_1, p_2, ...\}$ is the set of processors contained in locale e
 - Mems: $V \rightarrow \mathcal{P}(M)$ is the memory resource function
 - *M* is the set of memories (RAMs or caches)
 - $Mems(e) = \{m_1, m_2, ...\}$ is the set of memories contained in locale e
 - Comm : $V \rightarrow \{$ distributed, shared $\}$ is the communication attribute function
 - distributed and shared denote respectively communication via message passing and memory reference
 - Comm(e) is the worst-case communication kind among elements of e
 - Require that no shared locale has a distributed sub-locale



$$P = \{p_1, p_2, p_3, p_4\}$$
$$M = \{m_1, m_2\}$$

Example Locale: 2 Hopper 24-core Nodes



locales = hierarchically partitioned address spaces
smaller locale = closer elements = cheaper communication



- Any processor can access any address space
- Speed of access is modeled by the *smallest enclosing locale* of a processor and the other processor or memory it accesses
- Equivalently, by the *lowest common ancestor node* in the corresponding Cartesian resource hierarchy







Teams: Hierarchical Processor Groups

- Teams are groups of hardware processors (cores)
- Nested sets of processors which are *relatively close* in communication cost
- Teams specify sets of processors and inherit sets of memories
- Teams serve as *abstract locales* to isolate application from hardware details
- A team is a Cartesian resource hierarchy $T = (V, E, A, \mathcal{K})$ where
- V is the set of subteams and E is the containment relation among them
- A = {Procs, Mems, Comm} just as for locales
- A team has a hierarchy map $m: V_T \rightarrow \mathcal{P}(V_H)$ where
 - *H* is the hardware locale (root)

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- m(r) is typically a sub-locale of the hardware locale, where r the root of T;
 it denotes the machine subset implementing T
- **Procs(r)** is the team's set of processors, possibly a subset of Procs(m(r))
- *m* describes how the team's processors are distributed on the machine
- Consider a team as a *hierarchy of processors*, with its memories just inherited from its associated locale:
 - Require $\forall t \in V$: Mems(t) = Mems(m(t))
 - These are the memories close to the team's processors
- A team is mapped to hardware by the map *m*



Teams: Locality-aware Parallelism

- Teams are resources for parallel execution
 - Not a set of images or threads, but a set of processors (w/ nearby memories)
 - Basic unit of parallelism: *spawn task on team* (controls execution locality at arbitrary grain)
 - Team's processors cooperate to execute in parallel all tasks spawned on it
 - Team's memories hold tasks' stack frames & heap-allocated objects (by default)
- Uniform model for all concurrency in HCAF
 - Task parallelism: like async/finish X10, Habanero, Chapel, CAF 2.0
 - Loop parallelism: iterations are spawned on current team like X10 ateach
 - Data parallelism: array intrinsics implemented as parallel loops
 - Both intra-node and inter-node spawning are supported
- Hierarchical work-stealing scheduler per team
 - Similar to place schedulers in Habanero's Hierarchical Place Trees
 - Both distributed-memory and shared-memory work stealing are supported
 - Problem: lexical closures Habanero/Chapel style {in, out, inout} specifiers?
 - Implementation
 - Berkeley HotSLAW; Quintin & Wagner; Olivier & Prins; Saraswat, Paudel et al; etc

Coarrays: Hierarchical Data Objects

Coarrays are tiled groups of storage locations (elements)

- Nested tiles of elements which are *relatively close* in communication cost
- · Coarrays specify sets of elements and inherit processors and memories
- Coarrays are *allocated on teams* and their tiles are placed in teams' memories
- A coarray is a tiled resource hierarchy $C = (V, E, \mathcal{K}, A, \mathcal{T})$ where
- V is the set of sub-tiles and E is the containment relation among them
- A = {Elems, Procs, Mems, Comm} where Elems → storage locations in each tile
- Elems(r) is the coarray's top level (global-view) tile and $\mathcal{T}(r)$ is the tile's shape
- A coarray has a hierarchy map $m: V_C \rightarrow \mathcal{P}(V_T)$ where
 - T is the team on which C is allocated

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- m(r) is typically the root of the team, where r is the root of C
- *m* describes how the coarray's tiles are distributed on the team
- Consider a coarray as a *hierarchy of elements*, with its processors and memories just inherited from its associated team:
 - Require $\forall c \in V_C$: Procs(c) = Procs(m(c)) and Mems(c) = Mems(m(c))
 - These are the processors owning and memories storing the coarray
- A coarray is mapped to hardware by the composition $C \rightarrow T \rightarrow H$





Example: Coarray on Team on 2 Hopper Nodes



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- Overview
- HCAF Hierarchy Model
- Hierarchical Abstractions
- Language Constructs
 - Tiling patterns & generic hierarchy
 - Hierarchical teams
 - Hierarchical coarrays
 - Task, data, and SPMD parallelism
 - Example: Naive Matrix Multiply

Tiling Patterns

- Problem:
 - Locality-aware applications and optimizers statically depend on hierarchy shape
 - Hardware hierarchy is known only at runtime (cf. machine type & job scheduler)
 - Need abstraction to decouple application's virtual hierarchies from machine's real hierarchy
 - · But manually mapping virtual to real is difficult
- Solution:
 - Tiling pattern describes a set of desirable hierarchies
 - · Compiler statically optimizes using properties common to all set members
 - Runtime *dynamically chooses* desirable hierarchy with a *good mapping* to hardware
- Tiling pattern specifies:
 - Hierarchy rank (first d levels) and set of hierarchy coshapes
 - Required communication kind at each level (distributed vs shared memory)
 - Tile distributions and Rubik-style tilts/shifts/etc
- Example tiling pattern 'P' with hierarchy rank (2,1):



Tiling Patterns: Level & Dimension Specs



Tiling Patterns: Level & Dimension Specs



Tiling Patterns: Parameters & Constraints

• Parametrized pattern specifies a set of hierarchies

- · Parameters are positive integer variables local to pattern
- · Constraints are arithmetic predicates over parameters
- An *instantiation* is an assignment of values to parameters s.t. all constraints are satisfied
- Pattern matching:
 - Given hierarchy H, pattern P, and input tile T, find instantiation P' of P and H' = tiling(T, P') s.t. \exists "good" mapping $M : H' \rightarrow H$
 - Result is (H', M)
- Implicit parameter = unnamed param + constraint
 - Range: expr . . expr
- Extents in dimension-specs are Fortran exprs
 - Treated like array bound expressions
- Dimension-specs have lower and upper bounds
 - Like array bounds: extent : extent
 - Empty lower bound ≡ 1, empty upper bound ≡ *any*
 - 0 : 7..15 \Rightarrow 8 \leq *n* \leq 16 elements indexed from 0
 - \Rightarrow *n* > 0 elements indexed from 1



Tiling Patterns: Distribution & Comm Specs

• **Distribution specifier** modifies dimension-spec

- Specifies a dimension's assignment of elements to tiles i.e partially specifies T(c) at each child c of tiled node
- Classic distribution specs like HPF:
 - **block** contiguous w/ extent n or #n cyclic(k) cyclic over n w/ extent k
- Additional distribution specs like Rubik

tilt	tile boundary tilted
zigzag	tile boundary zig-zagged
zorder	space filling curve

- Default distribution is **block**, yields conventional tiling
- Communication specifier modifies level-spec
 - Specifies worst-case communication type at level
 ⇒ acts as a *constraint* in pattern matching
 - Types of communication:

distributed	message passing
shared	memory access

- **image** SPMD program instance (shared)
- any unspecified (the default)





Generic Hierarchy Operations

• H may be a locale, a team, or a coarray (some operations require hierarchy be regular)

- Shape and size
 - codepth(H)
 - corank(H), corank(H,k)
 - coshape(H), coshape(H,k)
 - cosize(H), cosize(H,k)
 - rank(H), rank(H,k)
 - shape(H), shape(H,k)
 - size(H), size(H,k)
- Access
 - H[i,j,...]
 - H[l:u:s,...]
 - H(i,j,...)
 - H(l:u:s,...)
- Locality
 - locale(H)
 - locale_info(id)
- Mapping
 - map_hierarchy(H,T)
 map_hierarchy(H,H2)

number of tiling levels ($0 \Rightarrow \text{leaf}$)

number of tile dimensions at top or specified tiling level tuple of tile extents at top or specified tiling level total number of tiles at top or specified tiling level number of element dimensions at top or specified tiling level tuple of element extents at top or specified tiling level total number of elements at top or specified tiling level

tile access tile section access element access element section access

opaque id of hardware locale to which H maps description of hardware locale identified by id

new hierarchy by tiling H with tiling pattern T new hierarchy by tiling H with tiling pattern of H2 $\,$

Constructs: Hierarchical Teams

- A *team* is a cartesian hierarchy of *processors* (not SPMD instances)
 - · Team's processors cooperate to execute tasks spawned dynamically on the team
 - Team's processors communicate and synchronize via collectives as in CAF 2.0
 - Teams are characterized by the (worst case) kind of communication available between processors
 - Distributed-memory team: communication by message passing
 - Shared-memory team: communication by memory access
 - Image team: communication by global variables
 - a shared-memory team within an execution of the SPMD program
 - Team characterization is determined by locale to which it is mapped

Team variable declarations

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- Recall that HCAF hierarchy types include a partial characterization of the hierarchy (i.e. of top *d* levels)
- So HCAF's type team is parametrized by a tiling rank:

team,	<pre>tiling[:,:]</pre>	::	t1
team,	<pre>tiling[:,:][:]</pre>	::	t2
team,	tiling(T)	::	t3

tiling rank is (2) tiling rank is (2,1) tiling rank is T's rank

Default tiling rank is "any":

```
team :: t
```

- rank is ()
- Team sub-typing by tiling rank subsumption:

```
t = t1
t1 = t2
t2 = t1
```

Allows static type checking of team variable uses

- ✓ since () is a prefix of (2)
- ✓ since (2) is a prefix of (2,1)
- **X** since (2,1) is not a prefix of (2)

Constructs: Hierarchical Teams (2)

Team construction

• Predefined team values:

TEAM_HARDWARE precisely describes hierarchy of current job's machine partition TEAM_WORLD as in CAF 2.0 (all processors, partitioned into image teams) TEAM DEFAULT as in CAF 2.0

• By splitting with a tiling pattern:

t3 = tile_map(TEAM_HARDWARE, T)

- By CAF 2.0's notion of team splitting?
 - Don't know how to make this work hierarchically

• Team usage

- Allocate a coarray on a team
- Perform collectives on a team
- Team-oriented control structures:
 - with team t as in CAF 2.0
 - with subteam t our version of Titanium team_split statement
 - select subteam t our version of Titanium partition statement case <stmt> ...
 end select

Data Parallelism: Parallel Loops

• Explicit data parallelism via loops

```
• Iterating over element indices of a coarray:
```

```
do parallel( i, j in A )
```

<statement list>

end

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Iterating over *tile* indices of a coarray:

```
do parallel( tile i, j in A )
```

<statement list>

end

• Iterating over part of a coarray:

```
do parallel( tile j in A[k,:] )
  <statement list>
and
```

end

• Loop indices can be omitted \Rightarrow rank-independent data parallelism

```
do parallel( tile in A )
      <statement list>
end
```

- Locality via hierarchy mapping:
 - Iterations of body are all spawned at once into implicit finish
 - Each iteration is spawned on the subteam owning the indexed element or tile

Task Parallelism: Async & Finish

- Two forms of async, analogous to Fortran's two forms of if
 - async(t) <statement>
 - async(t)

```
<statement-list>
```

- end async
- Can supply data reference instead of team \Rightarrow spawns on team owning the data
- Two forms of finish
 - finish <statement>
 - finish

```
<statement-list>
```

end finish

Additional event argument signals completion

```
• async(team = t, event = e) <statement>
```

• async(team = t, event = e)
 <statement list>

```
end async
```

What about SPMD Parallelism?

- What are the essential differences between task and SPMD parallelism?
 - Number of "program images"

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- Number of instantiations of libraries, number of copies of global variables
- This matters because program scope is special!
- Degree of parallelism present at startup
 - Task parallel => I control thread; SMPD parallel => P control threads
 - This matters because of data parallel loops:
 - are they fork/joins ?
 - or are they collectives ?
- Can SPMD be modeled as implicit an *initial fork* and a *final join* ?
- Can a data-parallel loop on a *distributed-memory* team have the same semantics as a data-parallel loop on a *shared-memory* team?
 - if not, how can we have one programming model with uniform semantics throughout the machine hierarchy?
- See following example for more insight

Example: Naive Matrix Multiply

```
program main
```

```
tiling :: T(m1, m2)
  [m1, m1]
  [m2, m2] shared
end
real, dimension(:,:), tiling(T) :: A, B, C
integer, parameter :: n = 1000
allocate( A(n,n), B(n,n), C(n,n) ) on(TEAM_HARDWARE)
! initialize A and B somehow ...
C = 0
call matmul(A, B, C)
```

end program

Example: Naive Matrix Multiply cont'd

```
subroutine matmul(A, B, C)
  real :: A(:,:)[#], B(:,:)[#], C(:,:)[#]
  integer :: n
  select tiling( A )
    case [:,:]
      n = cosize(A, 1)
      do parallel( tile i, j in C )
        do k = 1, n
          call matmul(A[i,k], B[k,j], C)
        end do
      end do
    case []
      n = size(A, 1)
      do parallel( i, j in C )
        do k = 1, n
            C(i,j) = C(i,j) + A(i,k) * B(k,j)
        end do
      end do
 end select
```

end subroutine